

# $\mathcal{P}$ , $\mathcal{T}$ -odd effects in YbCu, YbAg, and YbAu

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## ABSTRACT

In this work, the molecular enhancement factors of the  $\mathcal{P}$ ,  $\mathcal{T}$ -odd interactions involving the electron electric dipole moment ( $W_d$ ) and the scalar–pseudoscalar nucleon–electron couplings ( $W_s$ ) are computed for the ground state of the bimetallic molecules YbCu, YbAg, and YbAu. These systems offer a promising avenue for creating cold molecules by associating laser-cooled atoms. The relativistic coupled-cluster approach is used in the calculations, and a thorough uncertainty analysis is performed to give accurate and reliable uncertainties to the obtained values. Furthermore, an in-depth investigation of the different electronic structure effects that determine the magnitude of the calculated enhancement factors is carried out, and two different schemes for computing  $W_d$  are compared. The final values for the enhancement factors are  $(13.32 \pm 0.13) \times 10^{24} \frac{h \text{ Hz}}{e \text{ cm}}$ ,  $(12.19 \pm 0.12) \times 10^{24} \frac{h \text{ Hz}}{e \text{ cm}}$ , and  $(2.36 \pm 0.48) \times 10^{24} \frac{h \text{ Hz}}{e \text{ cm}}$  for  $W_d$  and  $(-48.63 \pm 0.53)h \text{ kHz}$ ,  $(-45.68 \pm 0.60)h \text{ kHz}$ , and  $(3.81 \pm 2.58)h \text{ kHz}$  for  $W_s$ , for YbCu, YbAg, and YbAu, respectively.

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## I. INTRODUCTION

The current best description of elementary particles and their interactions is given by the Standard Model (SM) of particle physics.<sup>1</sup> This model is capable of describing almost all experimental observations (excluding gravitational interactions) and of accurately predicting a wide range of diverse phenomena, which is why over time it has been consolidated as a well-tested physical theory. However, it does not address some important observed effects, such as the matter–antimatter asymmetry in the universe, the neutrino oscillations, and the existence and nature of dark matter and dark energy.<sup>2,3</sup> Over the past decades, many new theories and extensions of the SM have been proposed to explain these phenomena.<sup>3,4</sup> Testing and restricting these theories is important for advancing our understanding of the fundamental laws of physics.

A promising way to test some of these theories is to search for effects due to the simultaneous non-conservation of spatial ( $\mathcal{P}$ ) and time-reversal ( $\mathcal{T}$ ) parities in atoms and molecules, such as those arising from the electric dipole moments (EDMs) of electrons.<sup>5</sup> Interactions between these EDMs and electromagnetic fields violate both temporal and spatial invariances.<sup>6</sup> Within a  $\mathcal{CPT}$ -invariant theory ( $\mathcal{C}$  refers to charge-conjugation symmetry), if  $\mathcal{T}$  symmetry is violated, then the combined  $\mathcal{CP}$  symmetry must also be non-conserved so that clearly  $\mathcal{P}$ ,  $\mathcal{T}$  violation implies  $\mathcal{CP}$  non-conservation.<sup>2</sup>

The sources of  $\mathcal{CP}$  violation described by the SM lead to the prediction of a free-electron EDM  $d_e$  of  $\sim 5.8 \times 10^{-40} e \text{ cm}$ .<sup>7</sup> However, more sources of  $\mathcal{CP}$  violation beyond those predicted by the SM are needed to explain, for example, the observed matter–antimatter asymmetry. The additional sources of  $\mathcal{CP}$  violation would in turn

lead to an increase in the magnitude of the electron EDM (eEDM), even bringing it into the reach of present-day precision experiments.<sup>2</sup> Experimental searches for these phenomena are currently being carried out in atoms and molecules, taking advantage of the enhancement of the atomic and molecular EDMs. These arise from  $\mathcal{P}$ ,  $\mathcal{T}$ -violating interactions, mainly those taking place between the eEDMs and the large internal atomic or molecular electric fields, and also other  $\mathcal{CP}$ -odd nucleon–electron and nucleon–nucleon interactions.<sup>2,8–10</sup> Currently, the lowest upper limit of the eEDM is set at  $|d_e| < 2.1 \times 10^{-29} e \text{ cm}$ . This upper limit was reported after measurements conducted by the National Institute of Science and Technology (NIST) on the  $\text{HfF}^+$  molecular ion<sup>11</sup> and combining these results with those obtained by the ACME Collaboration in their analysis of the ThO molecule.<sup>12</sup> It is important to stress that if  $\mathcal{CP}$  violation is assumed to arise exclusively from  $d_e$  in the NIST experiment (i.e., if the scalar–pseudoscalar nucleon–electron couplings are neglected), then the upper limit would be  $|d_e| < 4.1 \times 10^{-30} e \text{ cm}$ . This lowest upper limit has already put considerable constraints on some of the theories beyond the SM.<sup>13,14</sup>

In the ground state of a molecule with zero nuclear spins and a single unpaired electron, there are two main contributions to the energy arising from  $\mathcal{P}$ ,  $\mathcal{T}$ -violating interactions, that is, the interactions between the EDMs of the electrons and the electromagnetic fields and from the  $\mathcal{P}$ ,  $\mathcal{T}$ -odd scalar–pseudoscalar nucleon–electron (S-PS-ne) neutral-current interactions.<sup>9,15</sup> Since the effects of the eEDM and the S-PS-ne interactions are enhanced by the molecular electronic structure, the two corresponding molecular enhancement factors  $W_d$  (related to  $d_e$ ) and  $W_s$  (which enhances the S-PS-ne interactions) are of particular interest.

The choice of molecule for the measurements has a significant impact on the sensitivity of the experiment due to, among others, the system-dependent enhancement of the  $\mathcal{P}$ ,  $\mathcal{T}$ -odd effects. Since in open-shell molecules that contain only one heavy element, this enhancement scales roughly as the cube of the atomic number of the heavier nucleus to which the unpaired electron is strongly linked to Refs. 10, 16, and 17, some heavy-element-containing molecules have an advantage over other systems. Furthermore, practical experimental considerations play a crucial role in selecting a candidate for experiments. For example, the use of ultra-cold molecules increases the interaction times and, hence, the experimental precision.<sup>18</sup> Therefore, the laser-coolability of the selected molecule provides a clear advantage. Various molecular properties relevant for precision measurements (e.g., laser coolability and sensitivity to the measured phenomena, but also many others) can be determined theoretically before experimental investigations in support of such experiments. In particular, the enhancement factors cannot be measured and must be provided based on accurate electronic structure calculations.

In this work, we investigate the sensitivity of the YbCu, YbAg, and YbAu molecules to  $\mathcal{P}$ ,  $\mathcal{T}$ -violating phenomena. These systems are of particular interest since they contain two metal atoms. Theoretically, this means that these atoms can be laser-cooled separately and then associated into a molecule afterward, eliminating the need to laser-cool the molecule as a whole.<sup>19–21</sup> So far, laser-cooling of Yb and Ag atoms has been demonstrated.<sup>22,23</sup> Laser-cooling of Cu and Au has not been demonstrated yet, but cooling schemes have been proposed.<sup>24</sup> Furthermore, these polar molecules have large molecular-frame electric dipole moments, due to the large

electronegativity of coinage-metal atoms, allowing for their easy polarization. In particular, YbAg is considered a promising candidate for a next-generation clock-transition eEDM measurement.<sup>21</sup>

No experiments have been performed so far on YbCu, YbAg, or YbAu, but several experimental groups pursue the ultra-cold formation of other Ag-containing molecules.<sup>25–28</sup> However, high-accuracy calculations of the potential energy curves, molecular-frame electric dipole moments, electric quadrupole moments, and static electric dipole polarizabilities of the present systems have recently been performed.<sup>29</sup> Here, we employ the four-component (4c) relativistic coupled-cluster (CC) approach to calculate the enhancement factors of the  $\mathcal{P}$ ,  $\mathcal{T}$ -violating interactions between the eEDMs and the electric fields in the systems,  $W_d$ , and of the  $\mathcal{P}$ ,  $\mathcal{T}$ -odd S-PS-ne interactions,  $W_s$ . The enhancement factors are determined for the ground states,  $X^2\Sigma^+_{1/2}$ , of the three molecules. We also carry out an extensive computational study to assign uncertainties to the calculated values.

In open-shell molecules containing at least one non-zero nuclear spin  $I$ , some internal nuclear interactions lead to nuclear spin-dependent molecular  $\mathcal{P}$ ,  $\mathcal{T}$ -violating effects, such as magnetic interactions between the electrons and the nuclear magnetic quadrupole moment (NMQM), which appears for nuclear spin  $I \geq 1$ .<sup>30,31</sup> These effects are, however, outside the scope of this work.

Section II covers the main theoretical aspects of this work, detailing how both enhancement factors can be obtained from effective Hamiltonians. Section III contains a description of the methods employed to calculate these factors, as well as the scheme used for geometry optimization. Next, Sec. IV presents the obtained enhancement factors and their dependence on effects such as the choice of the nuclear charge density model, the method for the treatment of electron correlation, the choice of the basis set, and the internuclear distances. Finally, Sec. V contains a concise summary of our findings.

## II. THEORY

The  $\mathcal{P}$ ,  $\mathcal{T}$ -violating interactions involving the EDMs of atoms or molecules produce non-zero linear Stark shifts in the limit of vanishingly small applied electric fields. These interactions originate from many different sources, but mainly from the EDMs of electrons and nucleons, as well as from the  $\mathcal{P}$ ,  $\mathcal{T}$ -violating nucleon–nucleon current interactions and the  $\mathcal{P}$ ,  $\mathcal{T}$ -odd electron–quark interactions.<sup>32</sup> In particular, for open-shell linear molecules in  $X^2\Sigma^+_{1/2}$  ground states, such as the systems treated in this paper, the interactions between eEDMs and electromagnetic fields and the  $\mathcal{P}$ ,  $\mathcal{T}$ -odd S-PS-ne neutral-current interactions dominate.<sup>33</sup> In these cases, the effective spin-rotation Hamiltonian that includes only nuclear-spin-independent  $\mathcal{P}$ ,  $\mathcal{T}$ -odd interactions (i.e., neglecting the interactions between electrons and NMQMs) can be written as<sup>9,34</sup>

$$\hat{H}_{\text{sr}}^{\mathcal{P}, \mathcal{T}\text{-odd}} = \left( \sum_K W_{s,K} k_{s,K} + W_d d_e \right) \hat{\Omega}, \quad (1)$$

where the  $\mathcal{P}$ ,  $\mathcal{T}$ -odd dimensionless operator  $\hat{\Omega} = \hbar^{-1} \mathbf{J}_e \cdot \mathbf{n}$  is the scalar projection of the reduced total electronic angular momentum operator  $\mathbf{J}_e / \hbar$  onto the unit vector  $\mathbf{n}$ . The direction and sense of this vector operator  $\mathbf{n} = \boldsymbol{\mu} / |\boldsymbol{\mu}|$  are given by the electric dipole moment of the system in the molecular frame,  $\boldsymbol{\mu}$ . For a linear

molecule, the direction of this unit vector is given by the internuclear axis, while its sense depends on the distribution of the nuclear and electronic charge densities in the reference frame attached to the molecule. Here,  $\hbar = h/(2\pi)$  is the reduced Planck constant. The sum in Eq. (1) runs over all the nuclei  $K$  in the system. In systems where one nucleus is significantly heavier than the other (and where the unpaired electron is mostly located on that heavy nucleus), this sum typically reduces to a single term. We also note that  $k_{s,K}$  is specific to each nucleus  $K$ , i.e., it depends on both the proton and neutron numbers. Both these points will become important later and are discussed in Sec. II B.

To compute the enhancement factors, the effects of the eEDM and the S-PS-ne interactions are taken as perturbations on the 4c relativistic Dirac–Coulomb (DC) Hamiltonian. Since  $d_e$  and  $k_{s,K}$  are small quantities, the effects arising from both interactions are minute. Therefore, first-order perturbation treatment will already yield highly accurate results.

Within the Born–Oppenheimer approximation, the 4c DC (clamped-nuclei) Hamiltonian is given by

$$\hat{H}^{(0)} = \sum_i \left[ c\alpha_i \cdot \hat{\mathbf{p}}_i + \beta_i m_e c^2 - \mathbb{1}_{4 \times 4} \sum_K e\Phi_K(\mathbf{r}_i) \right] - \mathbb{1}_{4 \times 4} \frac{1}{2} \sum_{i \neq j} e\Phi_j(\mathbf{r}_i) + \mathbb{1}_{4 \times 4} U^{\text{nuc}}, \quad (2)$$

where

$$\Phi_K(\mathbf{r}_i) = \frac{1}{4\pi\epsilon_0} \int \frac{\rho_K(\mathbf{r}')}{|\mathbf{r}_i - \mathbf{r}'|} d^3\mathbf{r}', \quad (3)$$

$$\Phi_j(\mathbf{r}_i) = -\frac{1}{4\pi\epsilon_0} \frac{e}{|\mathbf{r}_i - \mathbf{r}_j|}, \quad (4)$$

$$U^{\text{nuc}} = \frac{1}{8\pi\epsilon_0} \sum_{K \neq L} \frac{Z_K Z_L e^2}{|\mathbf{R}_K - \mathbf{R}_L|}. \quad (5)$$

In Eqs. (2)–(4), as well as in all this work, the SI system of units was used. Here,  $\mathbb{1}_{4 \times 4}$  is the  $4 \times 4$  identity matrix, the operator  $\Phi_K(\mathbf{r}_i)$  refers to the Coulomb electric potential produced by the nucleus  $K$  at the position of the  $i$ th electron, whereas  $\Phi_j(\mathbf{r}_i)$  is the electric potential created by electron  $j$  at the position  $\mathbf{r}_i$ . The last term in Eq. (2) is the potential energy arising from all the nucleus–nucleus Coulomb interactions. According to Gauss' law, and considering that the root-mean-square radius of any nucleus is about five orders of magnitude smaller than the distance between the centers of any two nuclei in a molecule, the repulsive potential energy arising from the interaction between two given nuclei (provided that their electric charge distributions are described by spherically symmetric functions) can be safely approximated as the interaction between two point-type nuclei with their total charges concentrated in their centers. This approximation is standard in molecular physics. In addition,  $c$  is the speed of light in vacuum;  $m_e$  is the electron rest mass;  $e$  is the elementary charge;  $\epsilon_0$  is the vacuum permittivity;  $\rho_K(\mathbf{r}')$  is the charge density distribution of nucleus  $K$  at an arbitrary position  $\mathbf{r}'$ ;  $Z_K$  and  $Z_L$  are the atomic numbers of nuclei  $K$  and  $L$ , respectively; and  $\mathbf{r}_i$ ,  $\mathbf{r}_j$ ,  $\mathbf{R}_K$ , and  $\mathbf{R}_L$  are the position vectors of the electrons  $i$  and  $j$  and nuclei  $K$  and  $L$ , respectively. Here and in what follows, the sums over  $i$  and  $j$  run over all the electrons in the molecule, whereas the sums over

$K$  and  $L$  run over all the nuclei of the system. In addition,  $\hat{\mathbf{p}}_i = -i\hbar\nabla_i$  is the linear momentum (vector) operator of electron  $i$ , while  $\alpha_i$  and  $\beta_i$  are the well-known  $4 \times 4$  Dirac matrices in standard representation for the same electron. In this representation, they are expressed as

$$\alpha = \begin{bmatrix} \mathbb{0}_{2 \times 2} & \boldsymbol{\sigma} \\ \boldsymbol{\sigma} & \mathbb{0}_{2 \times 2} \end{bmatrix}, \quad \beta = \begin{bmatrix} \mathbb{1}_{2 \times 2} & \mathbb{0}_{2 \times 2} \\ \mathbb{0}_{2 \times 2} & -\mathbb{1}_{2 \times 2} \end{bmatrix}. \quad (6)$$

Here,  $\mathbb{1}_{2 \times 2}$  and  $\mathbb{0}_{2 \times 2}$  are the  $2 \times 2$  identity and null matrices, respectively, and

$$\boldsymbol{\sigma} = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \hat{\mathbf{i}} + \begin{bmatrix} 0 & -i \\ i & 0 \end{bmatrix} \hat{\mathbf{j}} + \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \hat{\mathbf{k}} \quad (7)$$

is the vector of Pauli matrices, with  $\hat{\mathbf{i}}$ ,  $\hat{\mathbf{j}}$ , and  $\hat{\mathbf{k}}$  being the unit vectors in Cartesian coordinates and  $i = \sqrt{-1}$  being the imaginary unit.

### A. eEDM enhancement factor $W_d$

The effects on hydrogenic atoms arising from a  $\mathcal{P}$ ,  $\mathcal{T}$ -odd interaction between the permanent EDM of a single electron, parallel to its spin, and an electromagnetic field have been studied for the first time by Salpeter in 1958.<sup>35</sup> In his seminal work, he introduced a  $\mathcal{P}$ ,  $\mathcal{T}$ -odd perturbation term corresponding to a permanent eEDM into the one-electron Dirac equation in a Lorentz-covariant formulation. This term is analogous to the so-called Pauli moment interaction term (representing a QED interaction of the lowest order, for non-relativistic energies, between the electromagnetic field and the Pauli anomalous electric and magnetic dipole moments of the electron) but pre-multiplied by the pseudoscalar Dirac operator  $\gamma^5$  (see pp. 47–51 of Ref. 36).

In atoms or molecules with at least one electron whose spin is unpaired, the effects arising from these  $\mathcal{P}$ ,  $\mathcal{T}$ -violating interactions produce atomic or molecular (permanent)  $\mathcal{P}$ ,  $\mathcal{T}$ -violating electric dipole moments that may be significantly larger than that of a free electron. In the past, it has been shown that the  $\mathcal{P}$ ,  $\mathcal{T}$ -violating EDM of these many-electron systems is mainly influenced by the electrostatic interactions between the eEDM of the unpaired electron and the internal electric fields.<sup>37</sup> Therefore, when calculating the molecular enhancement parameter  $W_d$  [see Eq. (1)], it is possible to ignore effects such as the interactions between the eEDM and the magnetic fields and also the electron–electron Breit interactions.

When neglecting both, the interactions of the eEDMs with internal and external magnetic fields and the Breit interactions, the mean value of the Salpeter Hamiltonian can be equated to the expectation value of two different operators. One of these two effective Hamiltonians is the sum of only one-electron operators, while the other one also contains two-body operators. These two-electron contributions, however, are considerably smaller than the one-electron ones in that particular effective Hamiltonian, and as such, they can usually be safely neglected.<sup>8,37</sup>

Therefore, by employing any of these two effective Hamiltonians—denoted henceforth as scheme 1 (S1) and scheme 2 (S2)—to make theoretical predictions, one avoids having to treat the two-electron interactions of the Salpeter Hamiltonian, which are

not negligible. The first of these effective Hamiltonians (i.e., within S1) has the following form:

$$\hat{H}_{\text{eff-1}}^{\text{eEDM}} = -d_e \sum_i (\beta_i - \mathbb{1}_{4 \times 4}) \Sigma_i \cdot \mathbf{E}(\mathbf{r}_i), \quad (8)$$

where the operator vectors  $\Sigma_i$  are related to the Pauli spin matrices by the following expression:

$$\Sigma = \begin{bmatrix} \sigma & \emptyset_{2 \times 2} \\ \emptyset_{2 \times 2} & \sigma \end{bmatrix}, \quad (9)$$

and  $\mathbf{E}(\mathbf{r}_i)$  is the total electrostatic electric field at the position of electron  $i$ , given by

$$\mathbf{E}(\mathbf{r}_i) = -\nabla_i \left[ \sum_K \Phi_K(\mathbf{r}_i) + \sum_{j \neq i} \Phi_j(\mathbf{r}_i) + \Phi^{\text{ext}}(\mathbf{r}_i) \right]. \quad (10)$$

Here,  $\Phi^{\text{ext}}(\mathbf{r}_i)$  is the electrostatic potential produced by the external electric field at the position of electron  $i$ , whereas  $\Phi_K(\mathbf{r}_i)$  and  $\Phi_j(\mathbf{r}_i)$  are the potentials given in Eqs. (3) and (4). The sums over  $K$  and  $j$  in the first and second terms of Eq. (10) run over all the nuclei and all the electrons of the molecule, respectively.

In what follows, we neglect in Eq. (8) the effects arising from both external electric fields and the electric field produced by the electrons (i.e., the two-electron terms in  $\hat{H}_{\text{eff-1}}^{\text{eEDM}}$ ), as their contributions to the molecular enhancement factors have been shown to be only on the order of one percent for heavy-element containing systems.<sup>8,17,37</sup> In this way, the effective Hamiltonian of S1 can be expressed as

$$\hat{H}_{\text{eff-1}}^{\text{eEDM}} \approx -d_e \sum_{i,K} (\beta_i - \mathbb{1}_{4 \times 4}) \Sigma_i \cdot [-\nabla_i \Phi_K(\mathbf{r}_i)], \quad (11)$$

and if the nuclear charges are modeled using point-type density distributions (PN), then this effective Hamiltonian is given by the operator

$$\hat{H}_{\text{eff-1(PN)}}^{\text{eEDM}} \approx -d_e \sum_{i,K} \frac{Z_K e}{4\pi\epsilon_0} (\beta_i - \mathbb{1}_{4 \times 4}) \Sigma_i \cdot \frac{\mathbf{r}_i - \mathbf{R}_K}{|\mathbf{r}_i - \mathbf{R}_K|^3}, \quad (12)$$

where its dependence on the atomic number of the nuclei in the system is explicit.

The second effective eEDM Hamiltonian, within S2, implicitly includes only the two-electron interactions contained in the Salpeter formulation and is given by<sup>37,38</sup>

$$\hat{H}_{\text{eff-2}}^{\text{eEDM}} = i d_e \frac{2c}{e\hbar} \sum_i \beta_i \gamma_i^5 \hat{p}_i^2, \quad (13)$$

where  $\hat{p}^2 = -\hbar^2 \nabla^2$  and  $\gamma^5$  is the well-known Dirac matrix of dimension  $4 \times 4$ , defined as  $\gamma^5 = i\gamma^0 \gamma^1 \gamma^2 \gamma^3$ , with  $\gamma^0 = \beta$  and  $\gamma = \beta\alpha = \gamma^1 \hat{i} + \gamma^2 \hat{j} + \gamma^3 \hat{k}$ . In terms of the  $\sigma_{x,y,z}$  Pauli spin matrices,  $\gamma^0 = \sigma_z \otimes \mathbb{1}_{2 \times 2}$ ,  $\gamma^{1,2,3} = i\sigma_y \otimes \sigma_{x,y,z}$ , and then,  $\gamma^5 = \sigma_x \otimes \mathbb{1}_{2 \times 2}$ , where  $\otimes$  implies a Kronecker product. Therefore, in the Dirac standard representation,

$$\gamma^5 = \begin{bmatrix} \emptyset_{2 \times 2} & \mathbb{1}_{2 \times 2} \\ \mathbb{1}_{2 \times 2} & \emptyset_{2 \times 2} \end{bmatrix}. \quad (14)$$

Unlike the effective Hamiltonian  $\hat{H}_{\text{eff-1}}^{\text{eEDM}}$  of Eq. (11), which explicitly depends on the nuclear charge density distributions  $\rho_K(\mathbf{r})$ , the Hamiltonian  $\hat{H}_{\text{eff-2}}^{\text{eEDM}}$  given in Eq. (13) does not have a functional dependence on effects due to finite nuclear sizes. However, when perturbation theory is applied to calculate the molecular enhancement factor  $W_d$  using S2, these effects are implicitly accounted for through their explicit inclusion in the unperturbed Hamiltonian of the system,  $\hat{H}^{(0)}$ .

Furthermore, S2 only contains one-electron operators within an approximation in which both the magnetic interactions and the electron–electron Breit interactions are neglected, reducing the computational complexity. However, a drawback of this effective Hamiltonian is in the fact that the non-relativistic limit of its mean value is not zero, while that of the Salpeter Hamiltonian vanishes.<sup>39</sup> Furthermore, S2 does not allow for the analysis of separate nuclear contributions to the calculated  $W_d$  parameters. Meanwhile, within S1, the non-relativistic limit of  $W_d$  is zero. While S1 includes two-electron contributions [see Eq. (8)], these are much smaller than the corresponding one-electron counterparts<sup>17,37</sup> and can usually be neglected. Therefore, S1 allows us to study the effective contributions to  $W_d$  arising from each nucleus of the system, keeping the correct non-relativistic behavior, and using only one-electron operators.

The interactions of the eEDMs with the internal electric fields can be taken as a perturbation on the DC Hamiltonian  $\hat{H}^{(0)}$  of Eq. (2), and, in such a case, the total (perturbed) electronic Hamiltonian is written as

$$\hat{H}^d = \hat{H}^{(0)} + \lambda \hat{H}^{\text{eEDM}}, \quad (15)$$

where  $\lambda$  is the dimensionless strength of the perturbation and  $\hat{H}^{\text{eEDM}}$  can be replaced either by  $\hat{H}_{\text{eff-1}}^{\text{eEDM}}$  or by  $\hat{H}_{\text{eff-2}}^{\text{eEDM}}$ .

The corrections to the molecular electronic energy arising from the perturbed Hamiltonian can be obtained by using Rayleigh–Schrödinger perturbation theory. A Taylor series expansion of the ground-state energy solution of Eq. (15),  $E_\Omega^d(\lambda)$ , can be written around  $\lambda = 0$  as

$$E_\Omega^d(\lambda) = E_\Omega^{(0)} + \lambda E_\Omega^{d(1)} \Big|_{\lambda=0} + \frac{\lambda^2}{2} E_\Omega^{d(2)} \Big|_{\lambda=0} + \mathcal{O}(\lambda^3), \quad (16)$$

where the subindices  $\Omega$  indicate that the ground-state solutions  $|0\rangle$  of the unperturbed Hamiltonian  $\hat{H}^{(0)}$  in a given fixed molecular frame and spin state fulfill the condition  $\langle 0|\hat{\Omega}|0\rangle = \Omega$ . For YbCu, YbAg, and YbAu, it can be seen that  $|\Omega| = 1/2$ .<sup>29</sup> Furthermore, the energy  $E_\Omega^{(0)} = \langle 0|\hat{H}^{(0)}|0\rangle$  is the eigenvalue of the unperturbed Hamiltonian  $\hat{H}^{(0)}$  in the same molecular frame. When only the leading-order corrections are retained, and taking into account the relation between the effective spin-rotation Hamiltonian and the eEDM enhancement factor  $W_d$  given in Eq. (1), it can be shown that this parameter is given as

$$W_d = \frac{1}{\Omega} \frac{dE_\Omega^d}{d\lambda} \Big|_{\lambda=0} = \frac{1}{\Omega} \frac{d}{d\lambda} \left( \frac{d}{d\lambda} \langle 0^d|\hat{H}^d|0^d\rangle \right) \Big|_{\lambda=0}, \quad (17)$$

where  $|0^d\rangle$  is the ground-state solution of the perturbed Hamiltonian  $\hat{H}^d$ .



### B. S-PS-ne enhancement factor $W_s$

A second source contributing to the  $\mathcal{P}, \mathcal{T}$ -violating interactions involving the electric dipole moment of an open-shell polar molecule in a  $2^2\Sigma_{1/2}$  ground state is the  $\mathcal{P}, \mathcal{T}$ -odd S-PS-ne neutral-current interactions. Assuming that in each nucleus  $K$ , the proton and neutron density distributions are equal to each other and also equal to the normalized nuclear density distribution  $\rho_K(\mathbf{r})$ , the effective Hamiltonian that accounts for the four-fermion semi-leptonic interactions in the electron–nucleon sector (in the limit of infinitely heavy nuclei) can be written in terms of proton–electron and neutron–electron interaction constants  $k_s^p$  and  $k_s^n$ , respectively, as<sup>9,15,32</sup>

$$\hat{H}^{S\text{-PS-ne}} = i \frac{G_F}{\sqrt{2}} \sum_{i,K} (Z_K k_s^p + N_K k_s^n) \beta_i \gamma_i^5 \rho_K(\mathbf{r}_i), \quad (18)$$

where  $N_K$  is the number of neutrons in nucleus  $K$ ,  $G_F$  is the Fermi coupling constant [whose most recent value is  $G_F/(\hbar c)^3 = 1.1663787 \times 10^{-5} \text{ GeV}^{-2}$ , or equivalently  $G_F \simeq 2.222516 \times 10^{-14} E_h a_0^{340}$ ], and  $\rho_K(\mathbf{r}_i) = \rho_K(\mathbf{r}_i)/(Z_K e)$  is the normalized nuclear density distribution of nucleus  $K$  at the position of the  $i$ th electron, satisfying  $\int \rho_K(\mathbf{r}) d^3\mathbf{r} = 1$ . In addition,  $E_h$  and  $a_0$  are the Hartree energy and Bohr radius, respectively. By defining a factor  $k_{s,K} = k_s^p + (N_K/Z_K) k_s^n$ , we can rewrite Eq. (18) as

$$\hat{H}^{S\text{-PS-ne}} = \sum_K \hat{H}_K^{S\text{-PS-ne}} = i \frac{G_F}{\sqrt{2}} \sum_{i,K} Z_K k_{s,K} \beta_i \gamma_i^5 \rho_K(\mathbf{r}_i). \quad (19)$$

Making a treatment analogous to the one applied to the eEDM Hamiltonian, it is easy to see that the S-PS-ne Hamiltonian can also be taken as a perturbation (with field strength  $\lambda$ ) to the 4c DC Hamiltonian so that

$$\hat{H}^s = \hat{H}^{(0)} + \lambda \hat{H}^{S\text{-PS-ne}}. \quad (20)$$

By expanding the solution energy around  $\lambda = 0$ , the enhancement factor  $W_s$  can be obtained as

$$W_s = \frac{1}{\Omega} \sum_K \frac{1}{k_{s,K}} \left. \frac{dE_{\Omega}^{s,K}}{d\lambda} \right|_{\lambda=0}. \quad (21)$$

### III. COMPUTATIONAL DETAILS

The calculations reported in this work were performed using the DIRAC 19.0 program package.<sup>41,42</sup> The bond lengths were optimized using the exact two-component (X2C) Hamiltonian,<sup>43</sup> the single-reference coupled-cluster method with single and double excitations (CCSD), and the s-aug-v4z basis set.<sup>44–46</sup> The active space energy cutoffs for the virtual (unoccupied) and occupied orbitals were set to  $\pm 20E_h$ ,  $\pm 10E_h$ , and  $\pm 10E_h$  for YbCu, YbAg, and YbAu, respectively. A smaller active space was used for the heavier molecules since computing their bond lengths is computationally more intensive. The optimized internuclear distances for YbCu, YbAg, and YbAu are 2.7543, 2.8589, and 2.6524 Å, respectively. The bond length increases from YbCu to YbAg and then decreases from YbAg to YbAu due to relativistic effects. A non-relativistic treatment would show longer bonds for heavier systems.<sup>47</sup> The enhancement factors were computed for these calculated equilibrium internuclear distances.

The molecular enhancement factors  $W_d$  and  $W_s$  were calculated using the four-component DC Hamiltonian and the multi-reference Fock-space coupled-cluster method with single and double excitations (FSCC).<sup>48</sup> A multi-reference method is required for these calculations due to the challenging character of the ytterbium-containing molecules.<sup>49,50</sup> This method has been employed previously to study the enhancement factors of the  $\mathcal{P}, \mathcal{T}$ -violating interactions in YbOH<sup>51</sup> and YbCH<sub>3</sub>.<sup>52</sup> In addition, the FSCC implementation within the EXP-T program<sup>53,54</sup> was used to investigate the effects of including triple excitations.

The uncontracted Dyall's valence-only basis sets of double- $\zeta$  (v2z), triple- $\zeta$  (v3z), and quadruple- $\zeta$  (v4z) quality were employed.<sup>55,56</sup> In addition, the core–valence basis sets (cvXz,  $X = 2, 3, 4$ ) were used to examine effects arising from the correlation of core electrons.<sup>57</sup> These particular basis sets add tight functions with large exponents to the vXz basis sets. Finally, the augmented basis sets (s-aug-vXz) were employed to investigate how accurately the outer regions of the systems were described. The s-aug-vXz basis sets add a single diffuse function to each symmetry block.

Nuclear electric charge densities were modeled using point-type or spherically symmetric Gaussian distributions. For a given nucleus  $K$ , the charge density distributions corresponding to a point-type nucleus (PN) and a Gaussian-type nucleus (GN) are, respectively,

$$\rho_K^{\text{PN}}(\mathbf{r}) = Z_K e \delta(\mathbf{r} - \mathbf{R}_K) \quad (22)$$

and

$$\rho_K^{\text{GN}}(\mathbf{r}) = Z_K e \left( \frac{\zeta_K}{\pi} \right)^{3/2} e^{-\zeta_K |\mathbf{r} - \mathbf{R}_K|^2}. \quad (23)$$

Here,  $\delta(\mathbf{r})$  is the Dirac delta distribution and  $\zeta_K = 3/(2\langle R_{\text{nuc},K}^2 \rangle)$ , with  $\sqrt{\langle R_{\text{nuc},K}^2 \rangle}$  being the root-mean-square radius of the nucleus  $K$ , which can be obtained using the empirical relation  $\sqrt{\langle R_{\text{nuc},K}^2 \rangle} = (0.836 A_K^{1/3} + 0.570) \text{ fm}$ , where  $A_K$  is the mass number of the isotope of interest.<sup>58</sup> The most abundant isotopes were considered, i.e., <sup>174</sup>Yb, <sup>63</sup>Cu, <sup>107</sup>Ag, and <sup>197</sup>Au.

For calculations of  $W_s$ , identical nuclear models (either PN or GN) were used in both the  $\hat{H}^{(0)}$  and  $\hat{H}^{S\text{-PS-ne}}$  operators [see Eqs. (2) and (19)]. In addition, when  $W_d$  was calculated using S1, the PN model was employed in both  $\hat{H}^{(0)}$  and  $\hat{H}_{\text{eff-1(PN)}}^{\text{eEDM}}$  [see Eqs. (2) and (12)]. The GN models were not yet implemented in DIRAC within  $\hat{H}_{\text{eff-1}}^{\text{eEDM}}$ . Finally, computations of  $W_d$  within S2 were performed using either PN or GN models in the unperturbed Hamiltonian  $\hat{H}^{(0)}$ .

The enhancement factors were calculated by employing the finite-field method. In particular, by combining Eqs. (16), (17), and (21), it can be seen that they can be obtained by applying the two-point finite-field method, where

$$W_d \approx \frac{1}{\Omega} \frac{d}{de} \left[ \frac{E_{\Omega}^d(\lambda) - E_{\Omega}^d(-\lambda)}{2\lambda} \right] \quad (24)$$

and

$$W_s \approx \frac{1}{\Omega} \sum_K \frac{1}{k_{s,K}} \left[ \frac{E_{\Omega}^{s,K}(\lambda) - E_{\Omega}^{s,K}(-\lambda)}{2\lambda} \right]. \quad (25)$$

Since  $\hat{H}_{\text{eff}-1}^{\text{eEDM}}$ ,  $\hat{H}_{\text{eff}-2}^{\text{eEDM}}$ , and  $\hat{H}^{\text{S-PS-ne}}$  are  $\mathcal{T}$ -odd operators, they cannot be included at the level of SCF iterations using the DIRAC code. However, the total energy of the perturbed systems can be obtained by transforming the integrals of these operators from the (Dirac–Coulomb Hartree–Fock) scalar atomic primitive basis to the molecular spinor basis. Even though the applied algorithm is not yet described in detail in the literature, Ref. 59 provides some valuable information about the used formalism.

A field strength  $\lambda = 10^{-6}$  was set when studying both parameters  $W_d$  and  $W_s$  in YbCu and YbAg, whereas  $\lambda = 10^{-7}$  was used for the calculations involving YbAu.

Atomic units (i.e.,  $e = 1$ ,  $a_0 = 1$ ,  $\hbar = 1$ , and  $4\pi\epsilon_0 = 1$ ) were used in all the calculations. For  $W_d$ , the values obtained following Eq. (24) were converted to the units used throughout this work using a conversion factor equal to the atomic unit (a.u.) of the electric field  $E_h/(e a_0) = 1.243\,380\,059 \times 10^{24} \frac{\text{h Hz}}{e \text{ cm}}$ . To calculate  $W_s$  following Eq. (25), the energies  $E_{\Omega,K}^{\text{s,K}}(\pm\lambda)/k_{\text{s,K}}$  were obtained in a.u. as mean values of the Hamiltonian,

$$\hat{H}^{(0)} \pm \frac{\lambda}{k_{\text{s,K}}} \frac{\sqrt{2} E_h a_0^3}{G_F Z_K} \hat{H}_K^{\text{S-PS-ne}}, \quad (26)$$

and then, the factor  $G_F Z_K/(\sqrt{2} a_0^3) = Z_K 0.103\,403\,426 \text{ h kHz}$  was used to convert the values of  $W_{\text{s,K}}$  from a.u. to h kHz. All values of the fundamental constants were taken from Ref. 40.

## IV. RESULTS AND DISCUSSION

To obtain accurate enhancement factors accompanied by well-defined uncertainties, multiple computational aspects will be addressed. For all the calculations discussed in this section, the 4c DC Hamiltonian was employed. First, the baseline results will be presented in Sec. IV A. Then, the effect of selecting two different nuclear charge density distribution models is examined for both factors in Sec. IV B. Furthermore, the two schemes employed for computing  $W_d$  will be compared in Sec. IV C. Next, the influence of the basis set will be determined in Sec. IV D. Thereafter, different computational approaches will be compared in Sec. IV E. Finally, the effect of the geometry of the system on  $W_d$  and  $W_s$  will be discussed in Sec. IV F.

This extensive investigation allows us to set uncertainties on the final values. The justification for the final results and their uncertainties will be given in Sec. IV G.

### A. Baseline calculations

All the reference values for  $W_d$  and  $W_s$  were computed on the v3z/FSCCD level, using the equilibrium bond lengths obtained in this work and Gaussian-type nuclear charge distribution models. The reference values for  $W_d$  have been obtained using S2 [see Eq. (13)]. For YbCu and YbAg, a virtual space cutoff of  $500E_h$  was employed, and two and four electrons were frozen, respectively. For YbAu, the virtual space cutoff was set to  $40E_h$ , and 56 electrons were frozen. The selection of these correlation parameters is justified in Table S1 of the supplementary material.

The calculated enhancement factors for the three systems are given in Table I. We can observe that both parameters are very similar for YbCu and YbAg, while much lower absolute values are obtained for YbAu. This finding will be elucidated in

**TABLE I.** Reference values of  $W_d$  (employing S2) and  $W_s$  for YbCu, YbAg, and YbAu. These results were obtained on the FSCCD/v3z level of theory, using Gaussian-type nuclear models, and freezing 2, 4, and 56 electrons, respectively.

Molecule	$W_d [10^{24} \frac{\text{h Hz}}{e \text{ cm}}]$	$W_s (\text{h kHz})$
YbCu	13.122	−47.647
YbAg	11.869	−44.361
YbAu	1.326	6.979

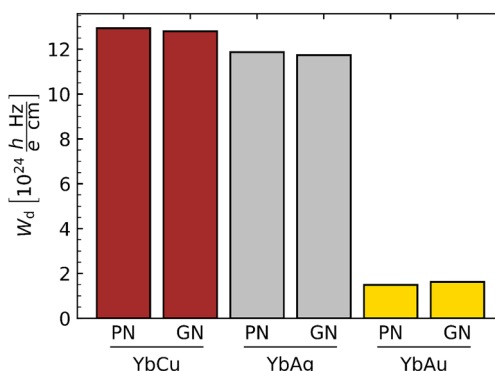
Sec. IV C. Furthermore, multiple corrections to these baseline values will be determined. The final obtained values will be given in Sec. IV G.

### B. Nuclear size effects

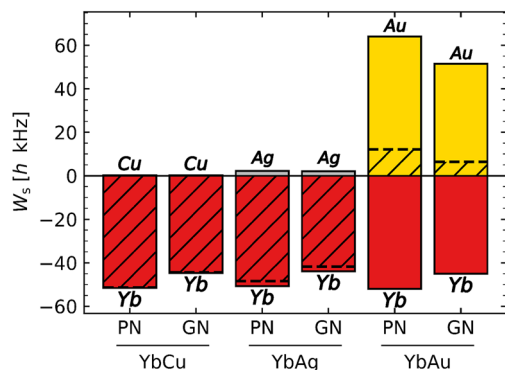
The effects arising from the use of two different nuclear models in the calculations of the molecular enhancement factors were investigated. For all three molecules, these effects were analyzed in both  $W_d$  and  $W_s$ . In this study, S2 has been employed to calculate  $W_d$ . All calculations were performed on the FSCCD/v2z level of theory, correlating all electrons and using a virtual space cutoff of  $3000E_h$  for all three systems.

In Fig. 1, the effects of using different nuclear charge density distribution models on  $W_d$  (S2) are shown (see also Table S3 of the supplementary material). For YbCu and YbAg, the results using GN are  $\sim 1.1\%$  smaller than those obtained employing PN, while for YbAu, the GN result is  $\sim 9.2\%$  larger than the PN one. In particular, the nuclear size effects on YbCu and YbAg agree with those on YbF previously reported by Gaul and Berger in Ref. 17. Employing S1, they modeled the internal electric field of Eq. (11) using PN and GN models (using in both cases GN to model the unperturbed Hamiltonian) and found that these two results for YbF differ by  $\sim 0.9\%$ .

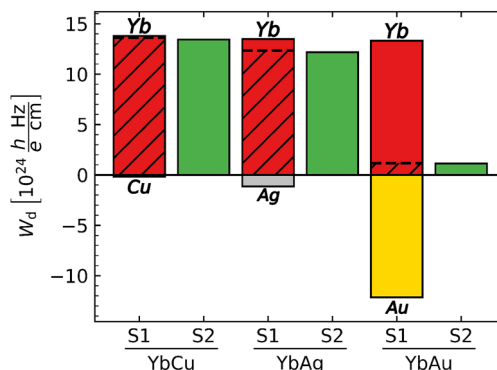
Meanwhile, in Fig. 2, the nuclear size effects on  $W_s$  are shown. The contributions from each of the nuclei are shown, as well as the total values of  $W_s$ , represented by hatched blocks. The contributions associated with the nuclei of the coinage metals become increasingly important as their atomic number increases. Moreover,



**FIG. 1.** Graphical representation of  $W_d$  (S2) for YbCu, YbAg, and YbAu using PN and GN models. Results obtained on the FSCCD/v2z level of theory, correlating all the electrons and using a virtual space cutoff of  $3000E_h$ .



**FIG. 2.** Contributions to  $W_s$  for YbCu, YbAg, and YbAu, arising from each nucleus, using PN and GN models. Results obtained on the FSCCSD/v2z level of theory, correlating all the electrons and using a virtual space cutoff of  $3000E_h$ . The hatched blocks correspond to the sum  $W_{s,Yb} + W_{s,X}$  ( $X = \text{Cu, Ag, Au}$ ).



**FIG. 3.** Graphical representation of the behavior of  $W_d$  of YbCu, YbAg, and YbAu computed using S1 and S2. For S1, the contributions from both nuclei are shown as well as their sums (hatched blocks). These results were obtained on the FSCCSD/v3z/PN level of theory, with a symmetric virtual space cutoff.

as expected, these contributions are of opposite sign to those of ytterbium because the gradients of the nuclear densities have opposite directions in the region between the two nuclei. For YbAu, the two contributions almost cancel each other out, leading to a very small total value of  $W_s$  (see Table S4 of the [supplementary material](#)).

In all three cases, the contribution of the ytterbium nucleus is reduced by  $\sim 13\%$  when going from PN to GN, while for copper, silver, and gold, the reduction is  $\sim 0.16\%$ ,  $\sim 3.5\%$ , and  $\sim 20\%$ , respectively. Thus, the effect of using a finite nucleus model becomes more significant for the heavier elements, as can be expected. The total absolute  $W_s$  is also lower for the calculations performed using the GN model.

### C. $W_d$ : Comparison of schemes 1 and 2

It is well known that when the electric field produced only by the nuclei is taken into account in S1, the two schemes described in Sec. II A should yield similar results for  $W_d$ .<sup>37</sup> While the use of S2 is computationally less demanding, since it requires just a single calculation per system instead of the two that are required for each diatomic molecule, S1 allows us to examine the effective contributions arising from each nucleus. To study those individual contributions, we present (to the best of our knowledge) the first four-component results of  $W_d$  using the approximate effective Hamiltonian of Eq. (12), corresponding to the use of S1.

The molecular enhancement factors  $W_d$  were computed using both schemes (S1 and S2) on the FSCCSD/v2z level of theory, using the PN model. Symmetric cutoffs of  $500 E_h$ ,  $500 E_h$ , and  $40 E_h$  were employed for YbCu, YbAg, and YbAu (freezing 2, 4, and 56 electrons), respectively. It is worth mentioning that the differences between the values of  $W_d$  computed according to S1 and S2 (using GN for the unperturbed Hamiltonian and the internal electric field of the perturbation in S1) have been previously studied using two-component methods in a set of almost 30 diatomic molecules.<sup>17</sup>

In Fig. 3, we show the differences in  $W_d$  when computed with the two schemes for the three systems (see also Table S5 of the [supplementary material](#)). The values of  $W_d$  for YbCu and YbAg calculated using S1 are about 1.5% higher than those obtained using

S2; this difference is 5% for YbAu. These differences may arise from contributions due to two-electron interactions, which are not taken into account in our implementation of S1 but are implicitly included in S2, but also from our use of finite basis sets, which could lead to different representation qualities of the different involved operators. These contributions are on the order of 1% for molecules containing one predominant heavy element (YbCu and YbAg), in agreement with previous predictions.<sup>8,17,37,60</sup>

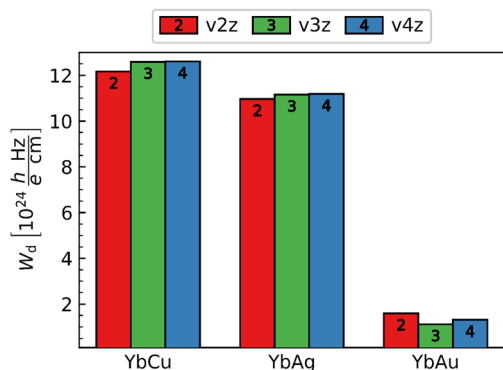
Using S1, it can be seen that the contributions to  $W_d$  from the Yb nucleus remain almost constant for all three systems. Moreover, the contributions from the coinage metals all have opposite signs to those coming from Yb, as is the case for the  $W_s$  factors. This is expected since the electric fields due to the two nuclei in the internuclear region have opposite directions, and according to Eqs. (11) and (12), this generates opposite contributions to this enhancement parameter. The decreasing total  $W_d$  factor from YbCu to YbAu is due to the increasing contribution from the second nucleus (opposite to that of the first).

### D. Basis set effects

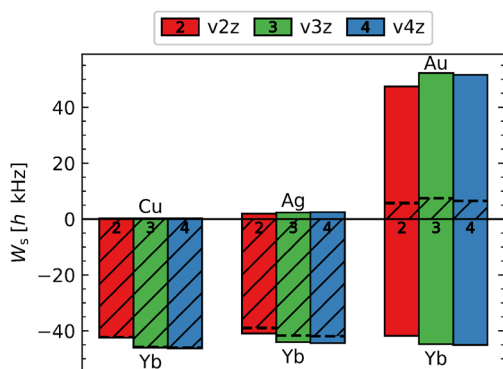
To observe how the size of the basis set influences the enhancement factors,  $W_d$  (S2) and  $W_s$  were computed with double- $\zeta$ , triple- $\zeta$ , and quadruple- $\zeta$  quality basis sets. These calculations were done using GN models, FSCCSD method, and the (occupied and virtual) active space cutoffs were set to  $\pm 20 E_h$ ,  $\pm 10 E_h$ , and  $\pm 10 E_h$ , freezing 38, 64, and 82 electrons of YbCu, YbAg, and YbAu, respectively.

The plot in Fig. 4 shows the effect of increasing the basis set cardinality on  $W_d$  (see Table S6 of the [supplementary material](#)). Deviations of at most 3.5% are observed when this enhancement factor is calculated for YbCu and YbAg using v2z and v4z basis sets, whereas these differences reduce to less than 0.5% when v3z and v4z results are compared. While no apparent convergence can be observed for the total  $W_s$  values of YbAu, this convergence can be seen by looking at the individual contributions in Fig. 5. A similar trend is expected for  $W_d$ .

Apart from adding contributing functions to all orbitals, it is also possible to add only tight or diffuse functions. Tight functions should increase the accuracy of the description of the core region



**FIG. 4.** The  $W_d$  (S2) enhancement factors of YbCu, YbAg, and YbAu, computed at the FSCCSD level of theory using GN models, and employing v2z, v3z, and v4z basis sets.



**FIG. 5.** The  $W_s$  enhancement factors of YbCu, YbAg, and YbAu, for v2z, v3z, and v4z basis sets, individual contributions from each nucleus. Computations were performed at the FSCCSD level of theory, using GN models. The hatched blocks correspond to the sum of the contributions from both elements.

of the system, while diffuse functions should improve the accuracy of the description of the valence region of the system. For these calculations, we used the cvXz basis sets, which contain higher angular momentum tight functions, and the s-aug-vXz basis sets, which augment a diffuse function per symmetry to the vXz basis set. These

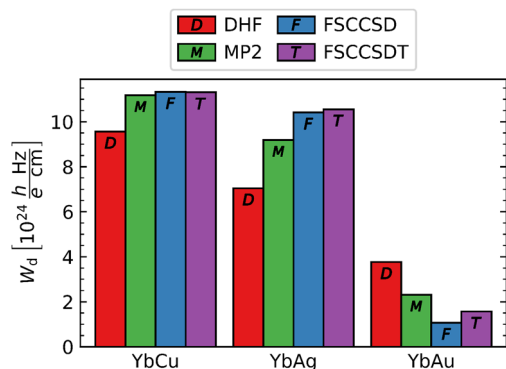
computations were done using the same computational settings as the ones above.

The effects arising from increased accuracy in describing the core and valence regions of the systems are small for both enhancement factors. Adding tight functions has a negligible effect on all three systems for  $W_d$  (with the largest change of 0.4%) and  $W_s$  (with the largest change of 0.3%). Meanwhile, adding diffuse functions reduces the parameter values slightly (with the largest changes of 2.9% and 1.9% for  $W_d$  and  $W_s$ , respectively). Furthermore, the enhancement factors of the YbAg system are more affected than those of YbCu. For YbAu, the addition of diffuse functions increases the calculated  $W_d$  and decreases the  $W_s$ . Still, the relative effects remain within 3% of the total value, as can be seen in Table S6 and Fig. S4 of the [supplementary material](#).

For the final calculations, the v3z basis set was used for baseline results, and then, corrections due to basis set quality and a better description of the core and valence regions were added. The incompleteness of the basis sets was also taken into account in the treatment of uncertainties.

### E. Electron correlation effects

The method used so far throughout this work for calculations of the enhancement factors was 4c Dirac–Coulomb FSCC. Other approaches to calculate  $W_d$  (S2) and  $W_s$  have been analyzed, and

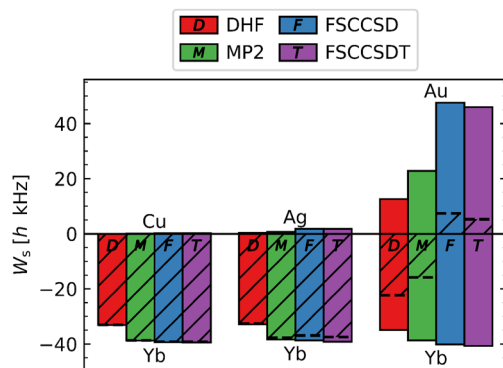


**FIG. 6.**  $W_d$  (S2) enhancement factors of YbCu, YbAg, and YbAu computed at DHF, MP2, and FSCC levels of theory, using GN models. These computations were performed using the v2z basis set, and the active space cutoffs were set to  $\pm 2E_h$ , freezing 66, 84, and 116 electrons of YbCu, YbAg, and YbAu, respectively.

**TABLE II.** Enhancement factors  $W_d$  (S2) and  $W_s$  of YbCu, YbAg, and YbAu computed at the DHF, MP2, and two different FSCC levels of approach. Computations were performed using the v2z basis set and GN models.

Method	$W_d [10^{24} \frac{h \text{ Hz}}{e \text{ cm}}]$			$W_s (h \text{ kHz})$		
	YbCu	YbAg	YbAu	YbCu	YbAg	YbAu
DHF	9.652	7.044	3.770	−33.081	−32.547	−22.275
MP2	11.174	9.188	2.314	−38.670	−37.696	−15.822
FSCCSD	11.323	10.415	1.072	−39.162	−36.897	7.385
FSCCSDT	11.310	10.555	1.567	−39.210	−37.406	5.268





**FIG. 7.**  $W_s$  enhancement factors of YbCu, YbAg, and YbAu computed at the DHF, MP2, and FSCC levels of theory, using GN models. Results from each nucleus are given separately. The hatched blocks indicate the combined values. These computations were performed using the same basis set and active space cutoffs as in Fig. 6.

the results are compared in Table II and Figs. 6 and 7. These methods are DHF, Møller–Plesset up to second order (MP2), FSCCSD, and FSCCSDT. The calculations were performed employing the dyall.v2z basis set and GN models, and the active space cutoffs for the post-DHF computations were set to  $\pm 2E_h$ , freezing 66, 84, and 116 electrons of YbCu, YbAg, and YbAu, respectively. This small active space and basis set were used because the inclusion of triple excitations (using the EXP-T program) is computationally expensive. The DHF results differ the most from the FSCC values, while the MP2 values are close to the FSCC results for YbCu and YbAg. Meanwhile, going from MP2 to FSCC reduces the value of  $W_d$  for YbAu by a factor of two and reverses the sign of  $W_s$ .

Including the triple excitations in the FSCC calculations has only a minor effect on the enhancement factors of YbCu and YbAg, but increases the  $W_d$  and decreases the  $W_s$  of YbAu significantly, in line with the enhanced sensitivity of these systems to the other computational parameters. It should be pointed out that due to the small size of the basis set, the contribution of the triple excitations should be considered as an order-of-magnitude estimate, rather than an accurate prediction. The differences between the FSCCSD and FSCCSDT methods will be used to estimate the uncertainty due to the neglect of the higher excitations in Sec. IV G.

## F. Influence of molecular geometry

### 1. Bond length corrections

The equilibrium bond lengths used in all the calculations of the enhancement factors reported so far were obtained in Sec. III, as no experimental bond lengths are available for the systems considered in this work.

To investigate the influence of the bond lengths on the enhancement factors, these parameters were computed at the calculated equilibrium internuclear distances reported in Sec. III (using S2 for  $W_d$ ), as well as at 0.05 and 0.1 Å larger and smaller internuclear distances. These computations were performed on the FSCCSD/v2z/GN level of theory, and the (occupied and virtual) active space cutoffs were set to  $\pm 100E_h$ ,  $\pm 100E_h$ , and  $\pm 95E_h$ , freezing 12, 20, and 28 electrons of YbCu, YbAg, and YbAu, respectively. The results are given in Table III. The absolute values of both enhancement factors of YbCu and YbAg decrease from the values at equilibrium bond lengths by less than 1.8% for the larger internuclear distance and increase by 2.2% at most for the smaller bond length. For YbAu, the deviations are significantly larger, up to 64%.

Given the strong (and almost linear) dependence of the enhancement factors on the internuclear distances (see Table III), the bond lengths of YbCu, YbAg, and YbAu were re-optimized so that some effects that were not accounted for previously (especially perturbative triple excitations and a larger active space) can be considered. Since there are no experimental internuclear distances for our systems, we first analyzed six molecules for which there are available measurements with which our optimizations can be compared: YbX ( $X = \text{F, Cl, Br}$ )<sup>61</sup> and YAu ( $Y = \text{Be, Mg, Ca}$ ).<sup>62–64</sup> These optimizations were performed using the Molpro package,<sup>65,66</sup> using a spin-free X2C Hamiltonian, ANO-RCC basis sets (with an effective cardinality larger than quintuple- $\zeta$ ),<sup>67–70</sup> and treating electron correlation effects by using the single-reference coupled-cluster method with a full treatment of single and double excitations and perturbative treatment of triple excitations [CCSD(T)], correlating all virtual orbitals and valence electronic orbitals (with a cutoff of  $-55$  a.u.). The use of a scalar-relativistic framework is justified here as these molecules are studied in the  $X^2\Sigma^+$  states. Our tests showed that the differences due to the neglect of spin-orbit effects are below 0.01 Å, i.e., smaller than the effects of basis set size and electron correlation, which we were trying to address.

**TABLE III.** Enhancement factors  $W_d$  (S2) and  $W_s$  of YbCu, YbAg, and YbAu, computed at different displacements ( $\delta_R$ ) with respect to the equilibrium bond lengths given in Sec. III. The computations were performed on the FSCCSD/v2z/GN level of theory.

$\delta_R$ (Å)	$W_d$ [ $10^{24} \frac{h \text{ Hz}}{e \text{ cm}}$ ]			$W_s$ (h kHz)		
	YbCu	YbAg	YbAu	YbCu	YbAg	YbAu
−0.10	12.739	11.623	0.756	−44.186	−41.423	10.193
−0.05	12.630	11.556	1.211	−43.805	−41.138	8.106
0.00	12.512	11.477	1.619	−43.390	−40.813	6.219
0.05	12.383	11.385	1.981	−42.940	−40.445	4.532
0.10	12.242	11.280	2.297	−42.451	−40.036	3.041

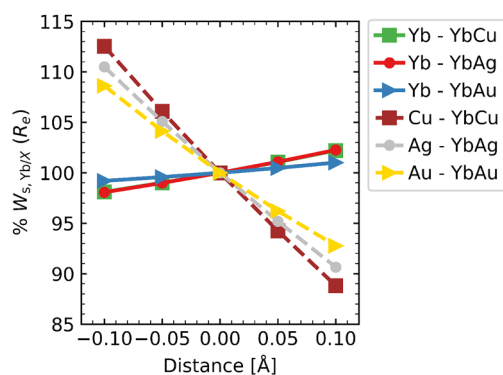
In all cases, these optimized bond lengths differ by less than 0.03 Å with respect to the available experimental values, with a mean absolute error of 0.012 Å (as can be seen in Table S11 of the [supplementary material](#)). Therefore, we can assume that the new internuclear distances obtained for YbCu, YbAg, and YbAu would have a similar error range. The same method was used to re-optimize the molecules of interest arriving at the final bond lengths of 2.7229, 2.8329, and 2.6975 Å for YbCu, YbAg, and YbAu, respectively. By fitting the enhancement factors and internuclear distances given in Table III with a linear function, we have corrected the values of  $W_d$  and  $W_s$  considering the new optimized distances. The results of these corrections are shown in Sec. IV G.

## 2. Vibrational corrections

The anharmonicity observed in the potential energy curves for the ground electronic states of YbCu, YbAg, and YbAu implies that their effective equilibrium bond lengths are slightly shifted compared to the minimum of the potential energy curves. These slight differences in bond lengths result in small changes in the enhancement factors.

To compute the vibrational corrections to  $W_d$  and  $W_s$ , calculations of these enhancement factors and the potential energies were performed for different bond lengths. The results for  $W_s$ , split up into contributions arising from each nucleus, can be found in Fig. 8 (and also in Table S8 of the [supplementary material](#)). These values are given as a function of the difference between the internuclear distances and the equilibrium bond length of the corresponding molecule. The resulting  $W_{s,Yb/X}$  values are shown as a percentage compared to the results found at the equilibrium bond lengths given in Sec. III. It can be seen that the coinage metal contributions are significantly more sensitive to the bond-length effects compared to the Yb contributions. This is also in agreement with the sensitivity of the respective atoms to the description of the electronic structure, as can be seen in Fig. 7 (and also in Table S7 of the [supplementary material](#)).

The vibrational corrections were computed using the VIBCAL module available in DIRAC-19.0, using a fourth-order polynomial for the energy fitting, and employing enhancement factors calculated at the equilibrium bond length given in Sec. III, 0.01, 0.05, and 0.1 Å larger and smaller internuclear distances. Scheme 2 was used to



**FIG. 8.** Effect of the internuclear distance on the enhancement factor  $W_s$  of YbCu, YbAg, and YbAu. These results were obtained on the FSCCSD/v2z/GN level of theory.

**TABLE IV.** Vibrational correction for both enhancement factors  $W_d$  ( $S_2$ ) and  $W_s$ . Results obtained on the FSCCSD/v2z/GN level of theory.

Molecule	$\Delta^{\text{vib}} W_d \left[ 10^{24} \frac{h \text{ Hz}}{e \text{ cm}} \right]$	$\Delta^{\text{vib}} W_s \text{ (h kHz)}$
YbCu	-0.032	0.115
YbAg	-0.024	0.086
YbAu	0.013	-0.048

compute  $W_d$ . The calculations were performed on the FSCCSD/v2z/GN level of theory, and the active space cutoffs were set to  $\pm 100E_h$ ,  $\pm 100E_h$ , and  $\pm 95E_h$  for YbCu, YbAg, and YbAu, respectively. The vibrational corrections are listed in Table IV for both enhancement factors, and they alter the baseline values of the enhancement factor (obtained at  $R_{eq}$ ) by <1%.

## G. Final values and uncertainties

The baseline results given in Sec. IV A can now be corrected to obtain the final values of  $W_d$  and  $W_s$ , which can also be considered as recommended values based on this work. The contributions due to using a larger basis set, correlating all electrons, increasing the virtual space cutoffs, including triple excitations in the FSCC method, and taking into account bond length and vibrational corrections were added to the reference baseline values. Table V and Table S9 of the [supplementary material](#) present the values of these different contributions and the final values.

The basis set corrections were calculated as differences between FSCCSD calculations with active space cutoffs of  $\pm 20E_h$  for YbCu and  $\pm 10E_h$  for YbAg and YbAu, employing the dyall.v4z and dyall.v3z basis sets (see Table S6 of the [supplementary material](#)).

The effects arising from correlating all electrons were taken as the differences between freezing 2, 4, and 56 electrons for YbCu, YbAg, and YbAu respectively, and correlating all the electrons and simultaneously increasing the virtual cutoff to  $6000E_h$  at the FSCCSD/v2z level of theory. A detailed analysis of the effects of the active correlation space size is also available in Sec. I of the [supplementary material](#).

The corrections due to the inclusion of higher excitations were taken as the differences between FSCCSDT and FSCCSD calculations, employing v2z basis sets and energy cutoffs of  $\pm 2E_h$ . Finally, the effects arising from the corrected bond lengths were taken as described in Sec. IV F 1, and the vibrational effects were extracted from Table IV.

To provide conservative and reliable uncertainties for these enhancement factors, a treatment similar to that given in Refs. 52, 71, and 72 was employed. The uncertainties obtained from the discussed considerations are given in Table VI and Table S10 of the [supplementary material](#) and analyzed individually in Subsections IV G 1–IV G 5.

### 1. Basis set

The uncertainties arising from the basis sets used in the calculations have three different sources: (i) the general quality of the basis sets (related to their cardinality), (ii) the number of extra tight functions, and (iii) the number of diffuse functions employed.

The overall quality of the basis sets affects the uncertainty of the final results because they cannot be considered fully converged at the v4z level. The baseline values are corrected by adding the

**TABLE V.** Final values of  $W_d$  (S2) and  $W_s$  for YbCu, YbAg, and YbAu, using GN models. The various corrections to the baseline values are assumed to be independent of each other.

	$W_d \left[ 10^{24} \frac{h \text{ Hz}}{e \text{ cm}} \right]$			$W_s \text{ (h kHz)}$		
	YbCu	YbAg	YbAu	YbCu	YbAg	YbAu
Baseline values	13.122	11.869	1.326	-47.647	-44.361	6.979
Corrections						
Bond length	0.078	0.045	0.347	-0.272	-0.180	-1.613
Vibrational effects	-0.032	-0.024	0.013	0.115	0.086	-0.048
Basis set cardinality (v4z vs v3z)	0.020	0.035	0.192	-0.269	-0.239	-0.983
Extra diffuse functions (s-aug-v3z vs v3z)	-0.001	-0.005	-0.033	0.002	0.012	0.143
Extra tight functions (cv3z vs v3z)	0.000	0.001	0.005	0.000	-0.006	-0.024
Active space <sup>a</sup>	0.149	0.135	0.016	-0.517	-0.483	1.478
Higher excitations <sup>b</sup>	-0.013	0.139	0.495	-0.047	-0.509	-2.117
Final values	13.323	12.195	2.361	-48.635	-45.680	3.815

<sup>a</sup>All-electron/ $+6000E_h$  vs  $\pm 500E_h$  (except for YbAu, where  $\pm 40E_h$  was the reference), with the v2z basis set.<sup>b</sup>FSCCSDT vs FSCCSD calculations, with an active space cutoff of  $\pm 2E_h$  and the v2z basis set.**TABLE VI.** Various sources of uncertainty for  $W_d$  (using S2) and  $W_s$  of YbCu, YbAg, and YbAu. The uncertainties are assumed to be independent of each other.

Uncertainty source	$ \delta W_d  \left[ 10^{24} \frac{h \text{ Hz}}{e \text{ cm}} \right]$			$ \delta W_s  \text{ [h kHz]}$		
	YbCu	YbAg	YbAu	YbCu	YbAg	YbAu
Bond length <sup>a</sup>	0.129	0.092	0.362	0.451	0.368	1.686
Basis set						
Basis set cardinality (v4z-v3z)	0.020	0.035	0.192	0.269	0.239	0.983
Extra diffuse functions (s-aug-v3z-v3z)	0.001	0.005	0.033	0.002	0.012	0.143
Extra tight functions (cv3z-v3z)	0.000	0.001	0.005	0.000	0.006	0.024
Electron correlation						
Virtual space cutoff <sup>b</sup>	0.019	0.016	0.005	0.061	0.054	0.003
Higher excitations <sup>c</sup>	0.007	0.070	0.248	0.024	0.255	1.059
Sum of $W_s$ approximation	...	...	...	0.059	0.308	1.313
Total uncertainty $\left( \sqrt{\sum_i (\delta_i W_{d/s})^2} \right)$						
Absolute uncertainty	0.132	0.122	0.480	0.532	0.596	2.584
Relative uncertainty (%)	1.0	1.0	20.3	1.1	1.3	67.7

<sup>a</sup>Calculated as  $|W_{d/s}(R_{eq} + 0.05 \text{ \AA}) - W_{d/s}(R_{eq})|$ . Values taken from Table III.<sup>b</sup>Taken as 0.5 of the difference between FSCCSD calculations using all-electron/ $+6000E_h$  and all-electron/ $+3000E_h$  (employing the v2z basis set).<sup>c</sup>Taken as 0.5 of the difference between FSCCSDT and FSCCSD calculations, with an active space cutoff of  $\pm 2E_h$  and the v2z basis set.

differences between the v4z and v3z results, as described in Sec. IV D, and also adding the differences between the s-aug-v3z and v3z results and between the cv3z and v3z values.

For both parameters, the uncertainties in basis set quality are seen to mainly arise from the differences between the v4z and v3z results. These differences are taken as the uncertainties related to the basis set cardinality.

The uncertainties due to the possible insufficient amount of tight functions were taken into account as the differences between

the cv3z and v3z results. Finally, the differences between the s-aug-v3z and v3z values were taken as the uncertainties in the treatment of diffuse functions.

## 2. Electron correlation

Electron correlation is affected by the chosen (occupied and virtual) active space cutoffs, along with the rank of excitations taken into account. To account for the frozen orbitals in the baseline calculations, the results provided in Table S1 and Figs. S1 and S2 of the

supplementary material are used. The differences in enhancement factors between correlating all electrons and freezing 2, 4, and 56 electrons for YbCu, YbAg, and YbAu, respectively, were used to correct the baseline values, as shown in Table V; we thus do not assign uncertainties related to not correlating all the electrons.

The corrections for the limited virtual space cutoff that is used in the baseline calculations are taken as the differences between the obtained values at virtual space cutoffs of  $6000E_h$  and  $500E_h$  for YbCu and YbAg and between  $6000E_h$  and  $40E_h$  for YbAu. The v2z basis set was used in these calculations, and the results are shown in Table V and also in Table S2 and Fig. S3 of the supplementary material.

To account for the effects of higher-lying virtual orbitals, half of the differences between the results obtained using virtual space cutoffs of  $6000E_h$  and  $3000E_h$  were taken as additional uncertainties (see Table VI).

The baseline values do not take into account triple excitations. The differences between the results obtained using FSCCSDT and FSCCSD methods, as described in Sec. IV E, were used to correct this omission. Since these results may not be fully converged yet, the effect of including triple excitations is used to estimate the uncertainty arising from not including quadruple and higher excitations, by multiplying by one-half the difference between the FSCCSDT and FSCCSD results.

### 3. Geometry

Inaccuracies in the calculated values of internuclear distances contribute to the enhancement factors' uncertainties. Based on our benchmark geometry calculations discussed in Sec. IV F 1, we conservatively set the uncertainty in the bond length to 0.05 Å

**TABLE VII.** Reference values of  $W_d$  and  $W_s$  for YbCu, YbAg, and YbAu compared to other ytterbium-containing molecules and systems currently or previously investigated experimentally to determine the lowest upper limits on  $d_a$  and  $k_s$ .

System	Source	$W_d [10^{24} \frac{h \text{ Hz}}{e \text{ cm}}]$	$W_s (h \text{ kHz})$
YbCu	This work	13.32(13)	-48.63(53)
YbAg	This work	12.19(12)	-45.68(60)
YbAu	This work	2.36(48)	3.81(258)
YbOH	Reference 51	11.32(48)	
	Reference 76	11.47	
	Reference 77	8.54 <sup>a</sup> ; 11.4 <sup>b</sup>	-30.8 <sup>c</sup> ; -41.2 <sup>d</sup>
	Reference 78	11.550	-41.318
	Reference 79	11.3 <sup>a</sup> ; 11.3 <sup>b</sup>	-40.9 <sup>c</sup> ; -40.9 <sup>d</sup>
YbCH <sub>3</sub>	Reference 52	13.80(35)	-50.16(127)
YbOCH <sub>3</sub>	Reference 80	11.6	
YbF	Reference 81	12.16	
	Reference 82		-41.2
	Reference 83	11.64	
	Reference 84	11.17(89)	
	Reference 85	11.23	-40.52(324)
	Reference 60	10.0 <sup>c</sup> ; 9.9 <sup>a</sup> ; 11.6 <sup>d</sup> ; 11.4 <sup>b</sup>	
	Reference 17	9.65 <sup>c</sup> ; 9.55 <sup>a</sup> ; 11.5 <sup>d</sup> ; 11.4 <sup>b</sup>	-34.6 <sup>c</sup> ; -41.2 <sup>d</sup>
	Reference 79	11.2 <sup>a</sup> ; 11.3 <sup>b</sup>	-40.6 <sup>c</sup> ; -40.9 <sup>d</sup>
HfF <sup>+</sup>	Reference 86	5.49	20.0
	Reference 79	5.66 <sup>a</sup> ; 6.36 <sup>b</sup>	20.7 <sup>c</sup> ; 23.4 <sup>d</sup>
ThO	Reference 87	20.31	116
	Reference 79	19.9 <sup>a</sup> ; 24.1 <sup>b</sup>	116 <sup>c</sup> ; 141 <sup>d</sup>
BaF	Reference 88	3.64	
	Reference 89	3.52	
	Reference 90	2.5	
	Reference 82		9.7
	Reference 60	2.9 <sup>c</sup> ; 2.9 <sup>a</sup> ; 3.3 <sup>d</sup> ; 3.3 <sup>b</sup>	
	Reference 17	2.91 <sup>c</sup> ; 2.87 <sup>a</sup> ; 3.33 <sup>d</sup> ; 3.28 <sup>b</sup>	7.58 <sup>c</sup> ; 8.67 <sup>d</sup>
	Reference 91	3.15(30)	8.35(70)
	Reference 71	3.13(12)	8.29(12)
	Reference 79	3.02 <sup>a</sup> ; 3.24 <sup>b</sup>	7.98 <sup>c</sup> ; 8.61 <sup>d</sup>

<sup>a</sup>ZORA, complex generalized Kohn–Sham.  $W_d$  with S2.

<sup>b</sup>ZORA, complex generalized Hartree–Fock.  $W_d$  with S2.

<sup>c</sup>ZORA, complex generalized Kohn–Sham.  $W_d$  with S1.

<sup>d</sup>ZORA, complex generalized Hartree–Fock.  $W_d$  with S1.



and calculate the enhancement factors for internuclear distances  $\pm 0.05$  Å around  $R_{\text{eq}}$  (see Table III). The resulting differences were taken as the uncertainties associated with the molecular geometry.

#### 4. Sum of atomic $W_s$ approximation

Since the interaction constants  $k_{s,K}$  in Eq. (19) are specific to each nucleus, calculating the total  $W_s$  value as a sum of the atomic contribution is only approximate and introduces an associated error. We analyze this error in detail in an upcoming publication.<sup>73</sup> Here, we provide the resulting uncertainties of  $0.059 h$  kHz,  $0.308 h$  kHz, and  $1.313 h$  kHz for YbCu, YbAg, and YbAu, respectively. We note that the specific errors differ for each isotopologue. Therefore, here, we use the isotopic average weighted by the natural abundances of all constituting elements.

#### 5. Total uncertainty

To compute the total uncertainties for the reference values of the enhancement factors of YbCu, YbAg, and YbAu, the Euclidean norm of the individual uncertainties is taken. These total uncertainties are obtained on the assumption that the different contributions are largely independent since they concern high-order effects.

The relative uncertainties for  $W_s$  are similar to those found for  $W_d$ . For these systems, the enhancement factors are dominated by the uncertainty on the bond lengths, followed by the uncertainties due to missing higher CC excitations and, to a smaller degree, by the basis set incompleteness. The calculated values of  $W_s$  and  $W_d$  of YbCu and YbAg have uncertainties of about a single percent. A similar computational approach yielded uncertainties of 2%–7% for the enhancement factors of BaF,<sup>71</sup> BaCH<sub>3</sub>, YbCH<sub>3</sub>,<sup>52</sup> and LaO, LaS, and LuO.<sup>72</sup>

The results for YbAu have significantly higher relative uncertainties than those of the other two systems. Both enhancement factors of this system are relatively small due to a cancellation of large similar-sized contributions from the two constituent atoms, rendering them very sensitive to computational settings and leading to large relative uncertainty.

#### H. Comparison with other systems

The calculated enhancement factors are compared to those found for other ytterbium-containing molecules in Table VII. In addition, some of the systems currently used in experiments aiming to restrict the lowest upper limit on the eEDM were added.<sup>11,12,74,75</sup> The  $W_d$  and  $W_s$  factors of YbCu and YbAg are of similar magnitude to those found for YbOH, YbCH<sub>3</sub>, YbOCH<sub>3</sub>, and YbF. Both enhancement factors of YbAu are significantly smaller than those found for any other ytterbium-containing systems.

Since both the interactions of the eEDMs with electromagnetic fields and the S-PS-ne neutral-current interactions may contribute to an eventual experimental detection of  $\mathcal{P}$ ,  $\mathcal{T}$ -violating effects in molecules, these two types of interactions should be decoupled from each other. This can be done by performing measurements on systems with different enhancement factor ratios.<sup>17</sup> For the systems studied in this work, and some other molecules currently and previously under investigation, these ratios can be calculated from the values of enhancement factors reported in Table VII.

#### V. CONCLUSION

Interpretation of experiments that search for  $\mathcal{P}$ ,  $\mathcal{T}$ -violating effects arising from both the interactions between eEDMs and electromagnetic fields and the S-PS-ne neutral-current interactions in molecules requires knowledge of the  $W_d$  and  $W_s$  enhancement factors, which can only be obtained through molecular electronic structure computations. In this work, these parameters were computed for the YbCu, YbAg, and YbAu systems, selected due to their possible experimental advantages. The enhancement factors  $W_d$  were calculated using two different schemes. This study confirms that, as indicated by previous predictions and studies,<sup>8,17,37,60</sup> the two-body contributions to  $W_d$  represent only about 1% of its value in the case of systems with a predominance of one heavy element (YbCu and YbAg) but reach up to 5% for YbAu, formed from two heavy elements. In addition, a thorough uncertainty analysis was performed to assign a conservative error to the obtained results.

The final values were calculated using the FSCC method and the 4c DC Hamiltonian in conjunction with relativistic basis sets. The main contributing sources of uncertainty are due to the limited basis set size and the neglect of CC excitations beyond triples.

The obtained enhancement factors of YbCu and YbAg are of very similar size to other Yb-containing compounds investigated in the literature. In the case of YbAu, the cancellation of the contributions arising from the two nuclei in the system leads to vanishingly small total  $W_d$  and  $W_s$  values. For YbCu and YbAg, the results are also of similar size as for other systems currently investigated experimentally to search for signs of  $\mathcal{P}$ ,  $\mathcal{T}$ -violating effects. Compared to YbF and YbOH, the alternate method of producing and cooling these systems provides an alternative route for future experiments setting a new lowest upper limit on the eEDM.

#### SUPPLEMENTARY MATERIAL

In the [supplementary material](#), we analyze the influence of the active space (in particular, of the energy of occupied and virtual correlated orbitals) on the calculation of  $W_d$  and  $W_s$ . We also present a set of tables where we report the values of these parameters using different nuclear models, different schemes corresponding to the use of the two effective Hamiltonians described in this work (for the case of  $W_d$ ), and a few different basis sets. In addition, tables are provided showing the dependence of the molecular enhancement factors on the use of different methods to treat electron correlation and vibrational effects and also the contributions to  $W_d$  and  $W_s$  associated with each nucleus of the studied molecular systems.

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## AUTHOR DECLARATIONS

### Conflict of Interest

The authors have no conflicts to disclose.

### Author Contributions

**Johan David Polet:** Data curation (supporting); Formal analysis (equal); Investigation (equal); Methodology (equal); Software (equal); Visualization (lead); Writing – original draft (lead); Writing – review & editing (equal). **Yuly Chamorro:** Conceptualization (equal); Formal analysis (equal); Investigation (equal); Methodology (equal); Software (equal); Supervision (equal); Validation (equal); Writing – original draft (supporting); Writing – review & editing (equal). **Lukáš F. Pašteka:** Conceptualization (equal); Formal analysis (equal); Funding acquisition (equal); Investigation (equal); Methodology (equal); Resources (equal); Software (equal); Validation (equal); Writing – review & editing (equal). **Steven Hoekstra:** Funding acquisition (equal); Investigation (supporting); Project administration (supporting); Resources (equal); Validation (supporting); Writing – review & editing (equal). **Michał Tomza:** Formal analysis (equal); Investigation (supporting); Methodology (equal); Writing – review & editing (equal). **Anastasia Borschevsky:** Formal analysis (equal); Funding acquisition (lead); Investigation (equal); Project administration (lead); Resources (equal); Supervision (equal); Writing – original draft (supporting); Writing – review & editing (equal). **I. Agustín Aucar:** Conceptualization (lead); Data curation (equal); Formal analysis (equal); Funding acquisition (equal); Investigation (lead); Methodology (equal); Resources (equal); Software (lead); Supervision (lead); Validation (equal); Visualization (supporting); Writing – original draft (equal); Writing – review & editing (lead).

## DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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